

There's something about a
fill - in - the - _____!

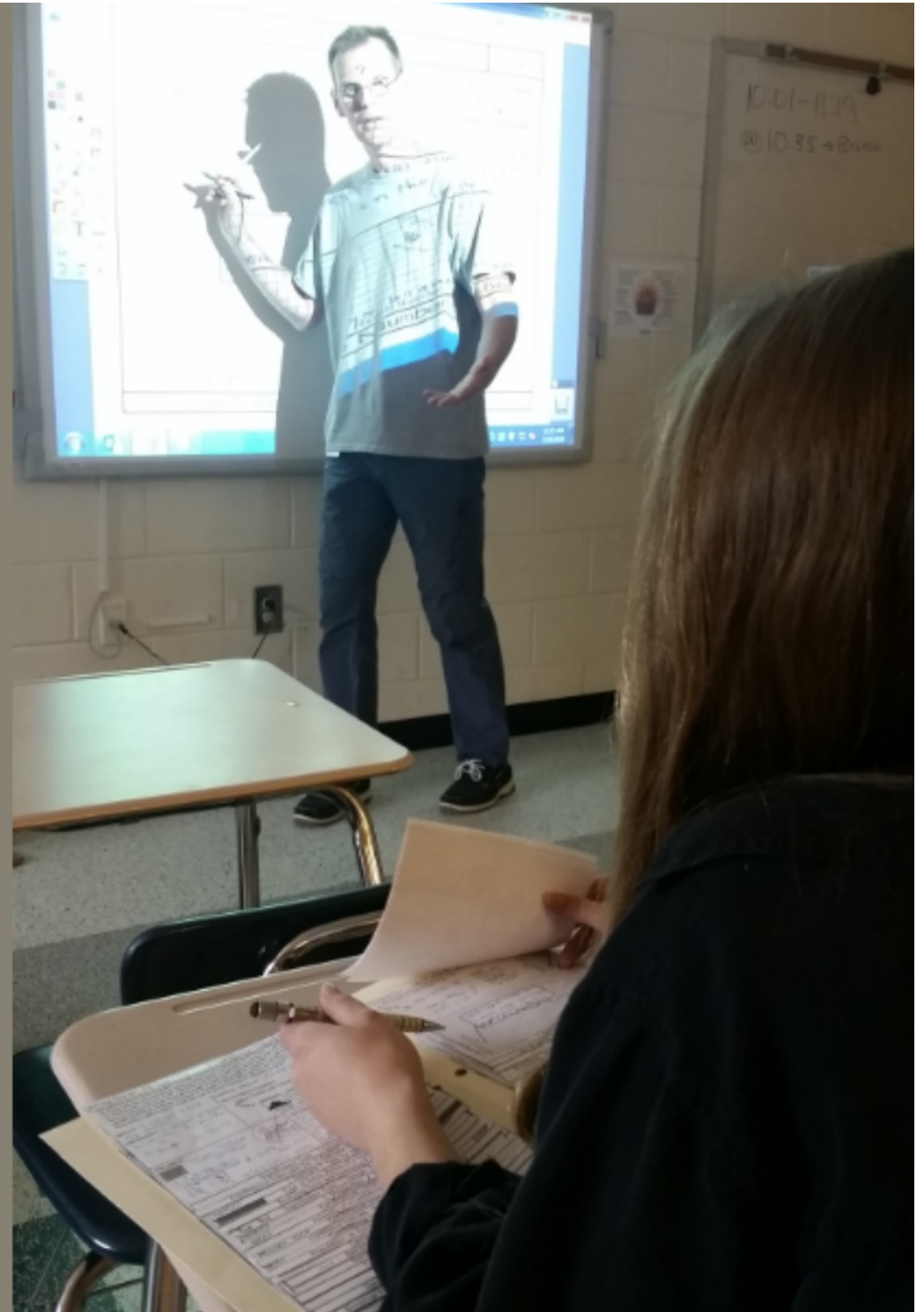


There's something about a
fill - in - the - _____ !

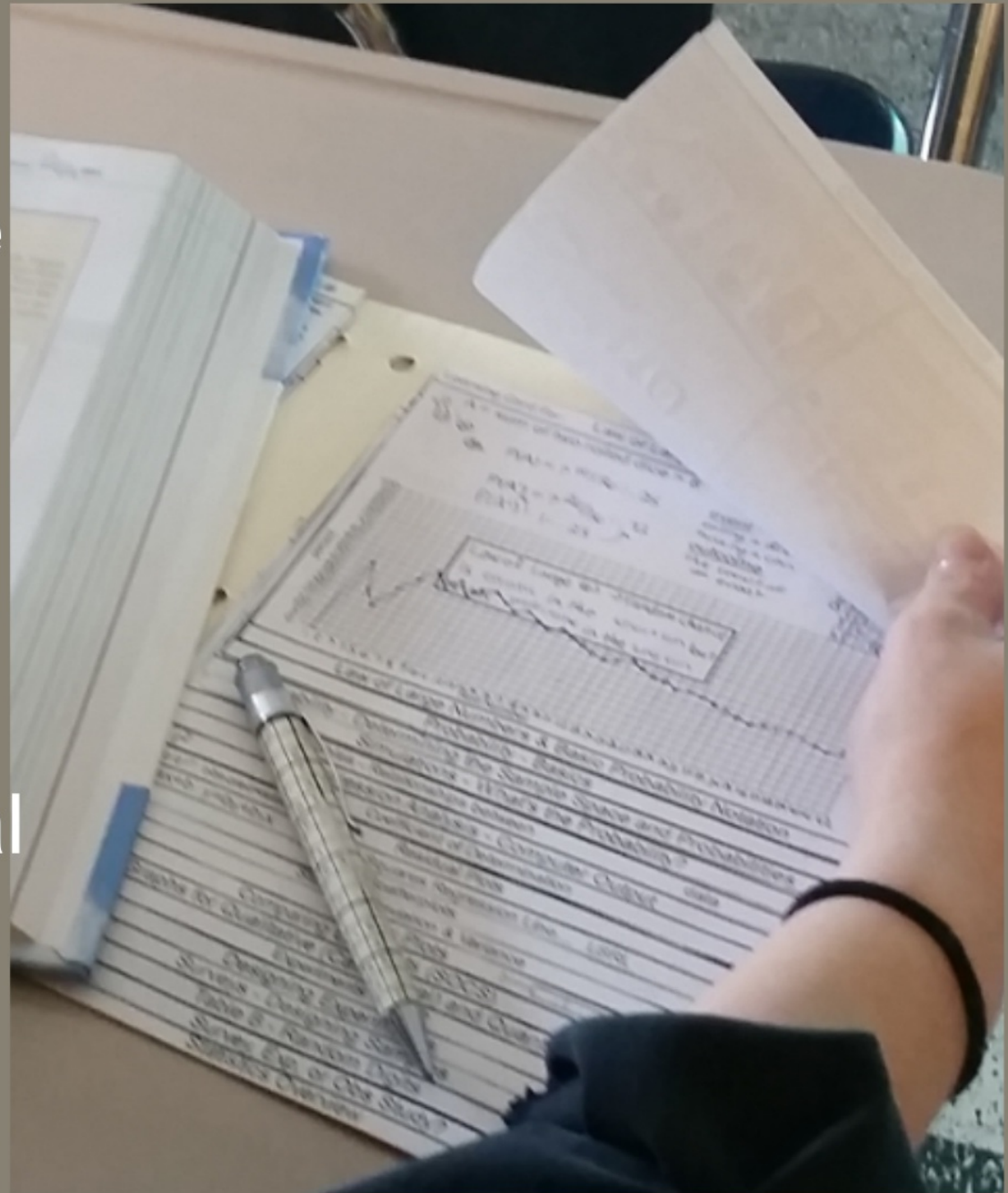
Blank



That's the idea
behind the learning
cards designed
specifically for AP
Statistics...



- structure to note taking
- reference for...
 - homework
 - classwork
 - unit tests, midterm & final
 - AP Exam
 - future courses



Learning Card for Survey, Exp, or Obs Study?

Name

Card #



Opinion



Best for _____

Need to select participants

_____ to avoid _____ in the results. We want a good _____ of the whole population.

Best for determining _____ & _____

- apply _____
- _____ decide which subjects get _____ vs. no _____.


To determine _____ between 2 _____

- usually working with _____ data OR if unethical and/or not _____ to experiment (example, smoking studies)
- no _____ with participants... _____ only!

Survey, Exp, or Obs Study?

Learning Card for Survey, Exp, or Obs Study? Name _____ Card # _____

Opinion




Best for _____

Need to select participants _____ to avoid _____ in the results. We want a good _____ of the whole population.

• apply _____ to decide which subjects get _____ no _____

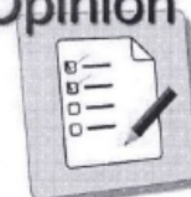


Best for determining _____ & _____



To determine _____ between 2 _____

- usually working with _____ data OR if _____ unethical and/or not _____ to _____ (example, _____)



Learning Card for Survey, Exp, or Obs Study?	Name	Key	Card #
<p>Surveys</p> <p>Opinion</p>  <p>Best for <u>opinions</u></p> <p>Need to select participants <u>randomly</u> to avoid <u>bias</u> in the results. We want a good <u>representation</u> of the whole population.</p>	<p>Experiments</p>  <p>Best for determining <u>cause & effect</u></p> <ul style="list-style-type: none"> • apply <u>treatments</u> • <u>randomly</u> decide which subjects get <u>treatment</u> vs. no <u>treatment</u>. • <u>Control group</u> ↗ 	<p>Observational Studies</p>  <p>To determine <u>Correlation</u> between 2 <u>variables</u></p> <ul style="list-style-type: none"> • usually working with <u>past</u> data OR if unethical and/or not <u>possible</u> to experiment (example, smoking studies) • no <u>interference</u> with participants... <u>observe</u> only! 	
Survey, Exp, or Obs Study?			

Learning Card for Survey, Exp. or Obs Study? Name Key Card # 1

Surveys Opinion Best for <u>opinions</u> Need to select participants <u>randomly</u> to avoid <u>bias</u> in the results. We want a good <u>representation</u> of the whole population.	Experiments Best for determining <u>cause & effect</u> • apply <u>treatments randomly</u> decide which subjects get <u>treatment</u> vs. <u>no treatment</u> • <u>Control group</u>	Observational Studies To determine <u>Correlation</u> between 2 <u>variables</u> • usually working with <u>past</u> data OR if unethical and/or not <u>possible</u> to experiment (example, smoking studies) • no <u>interference</u> with participants... <u>observe</u> only!
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Survey, Exp. or Obs Study?

Learning Card for Survey, Exp. or Obs Study? Name Key Card # 1

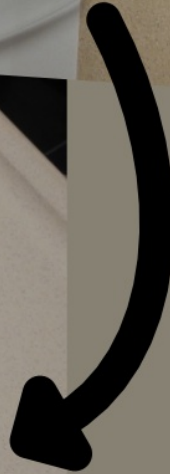
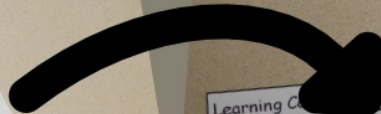
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Survey, Exp. or Obs Study?

Learning Card for Survey, Exp. or Obs Study? Name Key Card # 1

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Survey, Exp. or Obs Study?



binomial

getting exact

Distribution		1	2	3	4	5
0.0313	0.1875	0.3125	0.5	0.6875	0.8125	0.9688

← binomial ex (5, 1/2, 5)

cumulative always builds to 1

Calculating Mean and Std Dev

$\mu = np$

$\sigma = \sqrt{np(1-p)}$

$\mu = 5(0.5)$

$\sigma = 1.118$

$np \geq 10$

$n(1-p) \geq 10$



If the binomial meets these conditions, then we can use Normal distribution calculations (z-scores)

Binomial Formulas - pdf, cdf, mean, std dev, rules of thumb

Binomial Distribution

Random Variables

Continuous Random Variables

Assessing Normality

Probability Rules

Probability and Probability Models

DENSITY & PERCENTILES

Z-SCORES

PAST → PAST

use PAST to get an Z-value

Simulate - run the simulation & tall

using a random digits table or calculator

based

Conclusions → We estimate the probability to be 4 (number) runs.

Simulations - What's the Probability?

Lurking variables → Relationships between

Coefficient of Determination

Least Squares Regression Line... LSRL

Residual Plots

Scatterplots

Graphs for Qualitative (Categorical) and Quantitative Data

Experiments - Part 2

Designing Experiments

Surveys - Designing Samples

Statistics Overview

T-Test

Log & Log y or Ln(x & Ln(y))

Log(y)

Algorithms

Association/Independence?

Homogeneity of Pop S

Test for Homogeneity of Populations

Goodness of Fit Test for Categorical Data

Significance Tests - 1 Sample Paired T-Test (Means)

Significance Tests - 2 Sample T-Test (Means)

Significance Tests - 2 Proportion - Z Test

Type of Error, Power of a Test

Significance Tests - 1 Sample T-Test (Means)

Significance Tests - 1 Proportion - Z Test

Table C using degrees of freedom (n-1)

80%	90%	95%	96%	98%	99%
-----	-----	-----	-----	-----	-----

mean - t-interval

proportion - z-interval

REFLECT

order	Unit of Study	Learning Card Name
1	Introduction	statistics overview
2	Designing Studies	survey experiment or obs stud
3	Designing Studies	random digits table
4	Designing Studies	surveys – designing samples
5	Designing Studies	designing experiments
6	Designing Studies	experiments – part 2
7	Analyzing Data	graphs for qualitative and qua
8	Analyzing Data	comparing data sets (SOCS)
9	Analyzing Data	box plots
10	Analyzing Data	standard deviation
11	Analyzing Data	transforming data
12	Bivariate Data	scatterplots
13	Bivariate Data	least squares regression lines
14	Bivariate Data	residual plots
15	Bivariate Data	coefficient of determination
16	Bivariate Data	regression analysis – compute
17	Bivariate Data	2 way tables – categorical data
18	Probability	simulation
19	Probability	probability – determining the
20	Probability	probability – basics
21	Probability	law of large numbers
22	Probability	compound probabilities
23	Probability	conditional probabilities
24	Probability	venn diagrams
25	Random Variables	building a normal distribution
26	Random Variables	z-scores and normally distribu
27	Random Variables	z-scores and normally distribu
28	Random Variables	random variables – continuou
29	Random Variables	discrete – binomial settings
30	Random Variables	discrete – more on binomial settings
31	Random Variables	discrete – geometric settings
32	Random Variables	combining random variables
33	Sampling Distributions	sampling distributions – proportio
34	Sampling Distributions	sampling distributions – means
35	Sampling Distributions	central limit theorem – for means
36	Sampling Distributions	sampling distributions – bias and
37	Confidence Intervals	confidence intervals – anatomy c
38	Confidence Intervals	confidence intervals – proportio
39	Confidence Intervals	confidence intervals–means–sig
40	Confidence Intervals	confidence intervals–means–sig
41	Confidence Intervals	confidence intervals – reducing t
42	1 sample tests	1 proportion z-test
43	1 sample tests	1 sample t-test for means
44	1 sample tests	1 sample t-test for means – pai
45	1 sample tests	error types, power of a test
46	1 sample tests	reducing error and increasing p
47	2 sample tests	2 sample t-test for means
48	2 sample tests	2 sample confidence interval v:
49	2 sample tests	2 sample z-test for proportions:
50	2 sample tests	2 samp conf int vs 2 prop z tes
51	Chi Square tests	chi square – goodness of fit te
52	Chi Square tests	chi square – homogeneity of p
53	Chi Square tests	chi square – association/inde
54	Regression inference	linear regression inference
55	Regression inference	transformations – power
56	Regression inference	transformations – exponentia
57	Regression inference	transforming linear eqtns – p
58	Regression inference	linear regression – confidenc

Table of Contents – Learning Cards for AP Statistics

Mark Fisher
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original order	Unit of Study	Learning Card #	blank pdfs	filled out pdfs	iwb format	teacher notes
1	Introduction					
	Designing Experiments					

Learning Card for Designing Experiments

Name	Card #
Purpose of an experiment - Control Control Group Placebo effect Replication Randomization	Experimental Units Factors () Levels Treatment

Designing Experiments



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1	Introduction							
2								

Learning Card for Designing Experiments

Purpose of an experiment - to see if a specific treatment actually causes an effect.

Control... to minimize variability

Control Group - a group that does not receive the actual treatment.

Placebo effect - a response b/c you think you are getting an actual treatment.

Replication - multiple subjects; multiple studies

Randomization - randomly assigning subjects to treatment vs. control groups.

Experimental Units individuals to experiment on.

Factors - (explanatory variables) i.e. medicine

Levels - specific amounts of factors

Treatment - a specific condition applied to the units

Completely Randomized Design
 "Does this new drug really reduce coughing?"

60 Subjects → Randomly assigned → 30 - treatment group / 30 - control group → Compare results

example: ① Randomly assigned #'s to each participant ② Sorted #'s ③ first 30 #'s go to treatment group

*Be specific in how subjects were randomly assigned

Designing Experiments

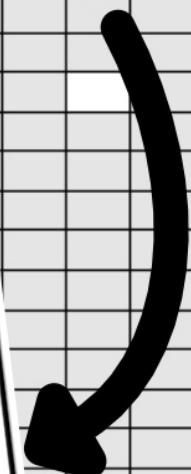


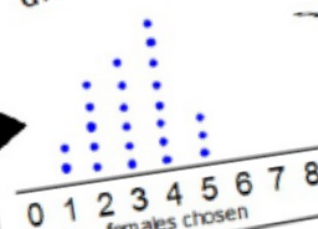
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1	Intro					

Learning Card for Statistics Overview Name _____ Card # _____

Use Probability...
 Was there discrimination?
 OR could this result just be due to random chance?



0 1 2 3 4 5 6 7 8
females chosen

Infer upon the population...
 if my sample shows tall people, then the true population is likely to have tall people "inference"

Probability

Inference

Data Production

Data Analysis

Analyze Data...
 Who are the individuals described?
 What variables?
 Why was the data collected?
 Where " " " "
 When " " " "
 How " " " "
 by Whom " " " "

Gather Data...
 from existing sources... internet, previous studies, etc.
 OR Produce it

- Surveys → opinions → no interference
- Observational studies → associations
- Experiments → apply treatments → cause and effect

Statistics Overview

Used results from the discrimination simulation activity for hiring pilots (male vs. female). Could use any simulation to see how variability naturally occurs based on random chance.

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3	Designing Stud...						

npr
 handwashing study - audio file - play this audio clip to emphasize the need to evaluate consequences of type 1 and type 2 errors.

stop at 1:43 and talk about research methods... experiment, obs study or survey? Why don't they do a survey?

continue audio to see which type of study it is

stop at 2:30... why so big? who pays for this study? why is the issue so important? lives at stake, billions of dollars in medical costs... which error type do you try harder to reduce?

Learning Card for \downarrow error, \uparrow power

So... you want to reduce type 1 errors!

α type 1	β type 2	Power ($1-\beta$)
\uparrow or \downarrow	\downarrow or \uparrow	\uparrow or \downarrow

4 ways to increase power

- * increase α
- * increase sample size
- * decrease σ (standard deviation)???
- * consider an alt. farther away from null???

Recall... $H_0: \mu = 325$ | $H_a: \mu > 325$
 null is true | alt is true

The power of the test is the power of the test to actually detect a difference if there is a difference!

Best advice to increase power... choose as high of an α level as you are willing to risk and as big of a sample size as you can afford

Reducing Error and Increasing Power of a Test

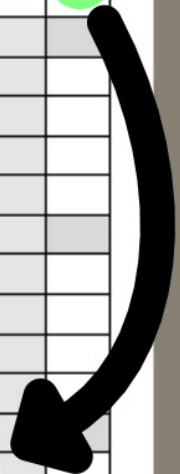


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8	Analyzing Data						
9	An						
10	An						
11	An						
12	Biv						
13	Biv						

iwb... "interactive white board"
 For import into Smart Board and other
 interactive white board programs.





P-value is low (.001) vs. ...
 So reject the null hyp of no
 correlation between crycount +
 IQ. There is strong evidence of
 a correlation between X + Y.
 slope ≠ 0 ? T-test



Interpretation

We are 95% Confident that the
 Interval of (.5, 2.5)
 Contains the true
 Parameter ($\beta \rightarrow$ slope)
 Stating that for every 1 increase in
 crycounts we predict IQ increases
 between .5 + 2.5.

Calculations

Estimate \pm (Critical Value \times Std. Dev.)

$b \pm t^* SE_b$ ← always given

$1.49 \pm 2.042(.487) \rightarrow (.5, 2.5)$
 use t-dist chart w/ df = n - 2

Coincides with the
 interpretation from the
 Linear Regression T-Test

plus

take note, zero is not in the
 interval... there is evidence of a correlation

CICP+ Inference for Linear Regression... Confidence Intervals 0 in the interval?

χ^2 (Chi Squared) Test for Homogeneity of Populations

Significance Tests - 2 Sample T-Test (Means)

NiHiCCI 1 Sample T Test for Means σ unknown

NiCCI...CICP Confidence Intervals - Mean σ known

Central Limit Theorem

Binomial Setting

Z-scores and Normally Distributed Data

Probability - Determining the Sample Space and Probabilities

Simulations - What's the Probability?

$y = ax + b$ $y = b_0 + b_1x$ Least Squares Regression Line... LSRL

Comparing Data Sets (SOCS)

Surveys - Designing Samples

Learning Card for Sampling Techniques

Name

Card #

population - everybody



census

or sample

(portion of the group)



Voluntary Response - individuals choose to respond - usually biased towards strong, negative opinions.

Convenience - Survey those who are easy to reach, can be biased.

Probability Samples

↳ groups must be representative of population

SRS (Simple Random Sample)

- names-in-a-hat
- everyone has equal chance
- every group of size n has equal chance

Stratified

- ① Divide population into groups based on an important characteristic
- ② Select a proportional SRS from each group or strata

Cluster

- ① Utilize existing groups or clusters that are easy to access.
- ② Randomly select groups
- ③ Survey everyone in the selected groups.

Systematic

- ① Randomly choose a starting point
- ② choose every n^{th} person after that.

! Cautions! !

- Response Bias - bias due to how you ask the question
- undercoverage - groups left out of your selection pool.
- nonresponse - bias b/c some refuse to participate or can't be contacted.

Inference to the Population

↳ getting good samples allows you to give accurate estimates of the overall population.

Surveys - Designing Samples

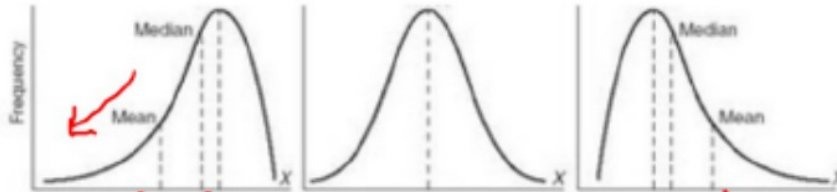
Comparing Data Sets (SOCS)

Learning Card for Comparing Data Sets

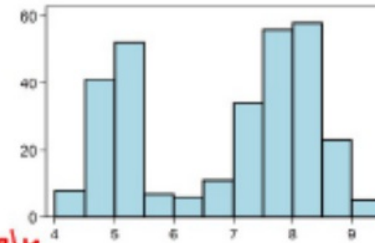
Name

Card #

Shape

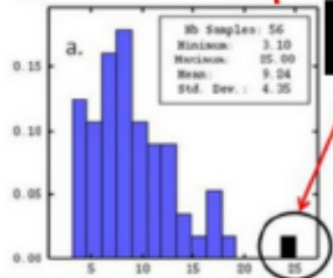


- skewed left
- unimodal
- skewed positively
- negatively skewed
- symmetrical
- unimodal or right 2 peaks = bimodal

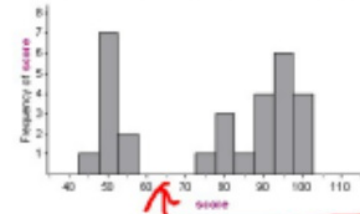


- uniform

Outliers (& unusual features)



1 outlier



a major gap in the data

Center

if symmetrical... use \rightarrow mean

if heavily skewed... use \rightarrow median

Spread

+ std. deviation

+ IQR / Range

Comparing Data Sets (SOCS)

nonresponse - bias b/c some refuse to participate or can't be contacted.

accurate estimates of the overall population.

What is it?

The line that best represents the linear relationship between 2 quantitative variables.

The line minimizes the residuals

$O - P = e$ equals R
 ↓ observed - predicted = residual

temp	clothing
degrees	pounds
25 deg	12.0 lb
40 deg	5.0 lb
60 deg	4.0 lb
83 deg	4.0 lb
104 deg	0.5 lb

How do I calculate it?

items needed: $\bar{x} = 62.4$ $S_x = 31.9$
 $\bar{y} = 5.1$ $S_y = 4.2$

$r = -.87$

① Calc slope $b_1 = r \frac{S_y}{S_x}$

$b_1 = -.87 \left(\frac{4.2}{31.9} \right) = -.115$

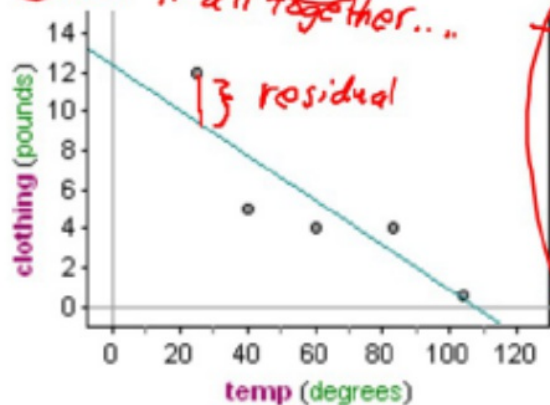
② Calc. y-intercept

$b_0 = \bar{y} - b_1 \bar{x}$

$b_0 = 5.1 - (-.115)(62.4)$

$b_0 = 12.3$

③ Put it all together...



How do I use it?

to interpret slope...
 For every increase of (x) 1 degree in temp. we predict that (y) pounds of clothing will decrease by .115

to interpret y-int...
 If zero degrees then the pounds of clothing is predicted to be 12.3
 to make predictions...
 if temp is 50, then...
 $\hat{y} = -.115(50) + 12.3$
 $\hat{y} = 6.6$

$y = ax + b$ $y = b_0 + b_1x$

Least Squares Regression Line... LSRL

undercoverage - groups left out of your selection pool. / accurate estimates of the overall population.
 nonresponse - bias by comparing Data Sets (SOCS)

Learning Card for Simulation

Name _____

Card # _____

Simulation... an imitation of chance behavior usually carried out with random numbers.

example:

3-way tie to be broken with coin flips. Each team tosses a coin. "Odd man out" meant that whichever team's result was different, that team is out. When all coins come up the same result, TV reporters seem amazed that this happens. What's the probability that all 3 coins come up the same? All heads or all tails?

State the problem or question at hand

State

Independent events? Other assumptions? equal chances, etc?

Ind?

Coin tosses are independent of each other; fair coins.

Map digit assignments state what each digit represents

Map

0-4 = Heads or even = heads
5-9 = Tails or odd = tails

Simulate run the simulation + tally the results

Simulate - using random digits table starting @ Line 101, ran 30 sets of 3 coin tosses →

same	diffn't
(10)	(20)

Conclude by answering the original question given your simulation results

Conclude - Coins came up the same one-third of the time... not that unusual

Simulations - What's the Probability?

Learning Card for

Sample Space

Name

Card #

To determine the sample space...

Make a random list

1,1 5,5 2,4

a systematic listing

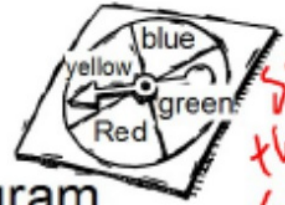
1,1 2,1 3,1
1,2 2,2 3,2
1,3 ...
...

2-way table (for 2 events)

Die #1	1	2	3	4	5	6
1	2	3	4	5	6	7
2	3	4	5	6	7	8
3	4	5	6	7	8	9
4	5	6	7	8	9	10
5	6	7	8	9	10	11
6	7	8	9	10	11	12

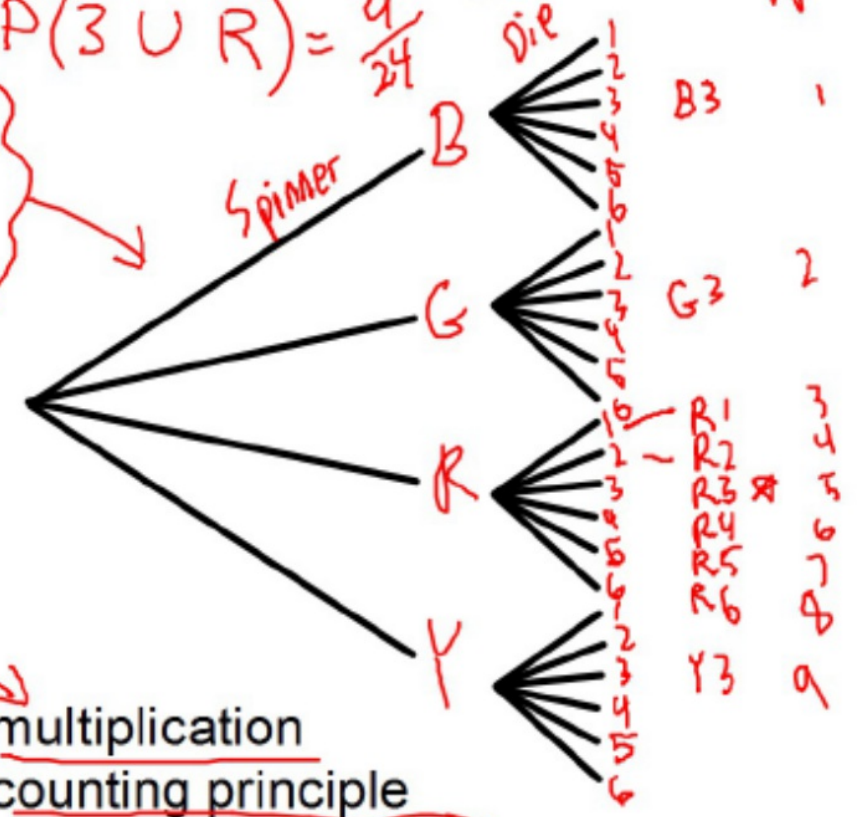


and



tree diagram

$P(3UR) = \frac{9}{24}$



Good for "What are the combos"

Good for "How many" questions

multiplication counting principle

$4 \times 6 = 24$

Probability - Determining the Sample Space and Probabilities

Comparing Data Sets (SOCs) of the overall population.

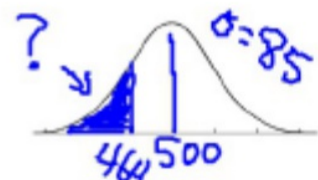
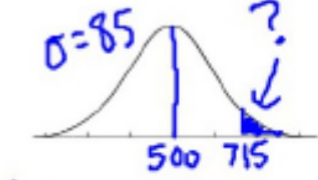
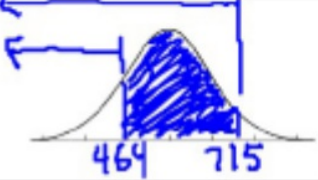
Surveys - Designing Samples

If... distributed

PSAT scores are normally distributed with a mean (μ) of 500 and a standard deviation (σ) of 85

μ population mean

σ population std. dev.

	Draw a Picture P icture	Standardize S tandardize	ASK the table or calculator A SK	Tell answer in context T ell																				
What proportion of students scored below 464?		$Z = \frac{x - \mu}{\sigma} = \frac{464 - 500}{85}$ $Z = -.42$	<table border="1" data-bbox="1323 698 1680 828"> <tr><td>z</td><td>.00</td><td>.01</td><td>.02</td></tr> <tr><td>-0.5</td><td>.3085</td><td>.3050</td><td>.3015</td></tr> <tr><td>-0.4</td><td>.3446</td><td>.3409</td><td>.3372</td></tr> <tr><td>-0.3</td><td>.3821</td><td>.3783</td><td>.3745</td></tr> </table>	z	.00	.01	.02	-0.5	.3085	.3050	.3015	-0.4	.3446	.3409	.3372	-0.3	.3821	.3783	.3745	33.72% of students scored below 464				
z	.00	.01	.02																					
-0.5	.3085	.3050	.3015																					
-0.4	.3446	.3409	.3372																					
-0.3	.3821	.3783	.3745																					
What proportion of students scored above 715?		$Z = \frac{x - \mu}{\sigma} = \frac{715 - 500}{85}$ $= 2.53$	$1 - .9943 = .0057$ <table border="1" data-bbox="1323 941 1680 1055"> <tr><td>z</td><td>.00</td><td>.01</td><td>.02</td><td>.03</td></tr> <tr><td>2.4</td><td>.9918</td><td>.9920</td><td>.9922</td><td>.9925</td></tr> <tr><td>2.5</td><td>.9938</td><td>.9940</td><td>.9941</td><td>.9943</td></tr> <tr><td>2.6</td><td>.9953</td><td>.9955</td><td>.9956</td><td>.9957</td></tr> </table>	z	.00	.01	.02	.03	2.4	.9918	.9920	.9922	.9925	2.5	.9938	.9940	.9941	.9943	2.6	.9953	.9955	.9956	.9957	.57% of students scored above 715.
z	.00	.01	.02	.03																				
2.4	.9918	.9920	.9922	.9925																				
2.5	.9938	.9940	.9941	.9943																				
2.6	.9953	.9955	.9956	.9957																				
What proportion of students scored between 464 & 715?		$715 \rightarrow .9943$ $464 \rightarrow .3372$ $.6571$	use info from tables above or normalcdf(-.42, 2.53, 0, 1) normalcdf(464, 715, 500, 85)	65.71% of students scored between 464 & 715.																				

Z-scores and Normally Distributed Data

How do I determine if it is a Binomial Setting?

It's a...

- S**uccess / Failure
each observation results in success or failure
- N**-observations - a fixed # of trials
- A**ll are independent
- P**robability of success for each trial has to be equal

B(n,p) **B(7,.5)**

Binomial Distribution

with n observations where each has the probability, p for Success.

Binomial Setting

Binomial Formula

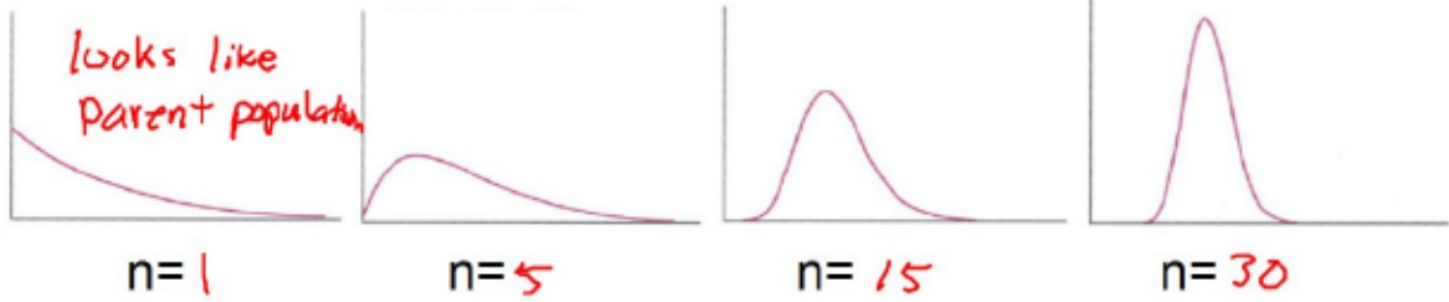
$P(X=k) = \binom{n}{k} P^k (1-p)^{n-k}$

Use Calculator to get the number of combinations of 6 successes from 7 trials... enter this... 7, math, prb, nCr, enter, 6, enter

$P(x=6) = \binom{7}{6} .5^6 (1-.5)^{7-6}$

$7C6 = 7(.5)^6(.5)^1$

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y=ax+b



The Central Limit Theorem discusses the Shape and only the Shape of the Sampling distribution of x when n is sufficiently large $\rightarrow n \geq 30$ *Sample size*

3 situations to consider:

Population has a normal dist. then the sampling dist. will be normal
 z-scores ✓
 Probabilities ✓ w/ normal dist.

non-normal pop dist, small n , then sampling dist. will be non-normal
 z-scores ✓
~~Probabilities w/ normal dist~~

non-normal pop dist, large n , then sampling dist. will be approx. normal
 z-scores ✓
 Probabilities ✓ w/ normal dist

Central Limit Theorem

Learning Card for

Name

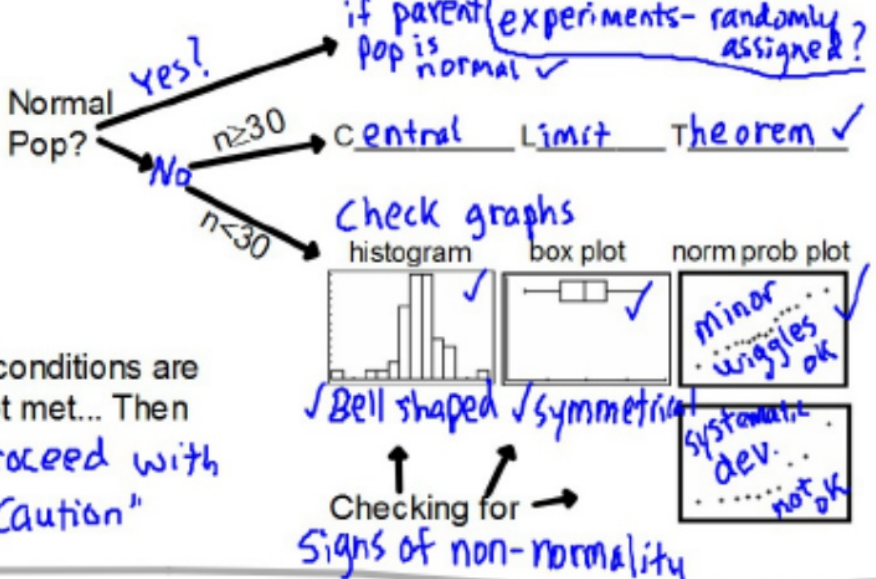
Card #

Name It

1-sample z-interval for means
 You sample 25 students using an SRS and get their average study hours per week of 5.3 hours. The population on study hours is normally distributed with a std dev of 1.2. Build a 95% confidence interval to estimate the mean study hours.

$\bar{x} = 5.3$ $n = 25$
 $\sigma = 1.2$

Conditions



Calculate $\bar{x} \pm z^* \left(\frac{\sigma}{\sqrt{n}} \right)$
 $5.3 \pm 1.96 \left(\frac{1.2}{\sqrt{25}} \right)$
 $(4.83, 5.77)$

Interpret

I am 95% Confident that the Interval 4.83 to 5.77 Contains true Parameter of mean study hours of the North Forsyth High Students
parameter of interest
context (overall population)

Confidence Level Interpretation: The method used to construct the interval will capture the true value about 95% of the time in repeated sampling

z* values	.674	.841	1.036	1.282	1.645	1.96	2.054	2.326	2.576	?
for Confidence Level "C"	50%	60%	70%	80%	90%	95%	96%	98%	99%	100%

NiCCI...CICP Confidence Intervals - Mean σ known

Least Squares Regression Line... LSRL
 Comparing Data Sets (SOCs) / of the overall population.

Surveys - Designing Samples

Name it & Hypothesize It!

1 Sample T-test for means

Ruffles Chips bag claims only 328mg of Olestra per serving. You eat a bunch; you get seriously sick; you want to sue Frito-Lay for incorrect labeling; you collect your own random sample of 35 bags and find a mean of 354mg with a sample std. dev. of 83.5mg. Can you win the lawsuit?

one-sided

two-sided

Null Hypothesis $H_0: \mu = 328$

Alternative Hypothesis $H_a: \mu > 328$

Statistical Signif (at level α) $\alpha = .05$

Calculations

$$\text{Test Statistic} = \frac{\text{Statistic} - \text{Parameter}}{\text{Std. dev of the Statistic}}$$

$$t = \frac{\bar{x} - \mu_0}{\frac{s_x}{\sqrt{n}}} = \frac{354 - 328}{\frac{83.5}{\sqrt{35}}} = 1.84$$

$$P(t > 1.84) = .037$$

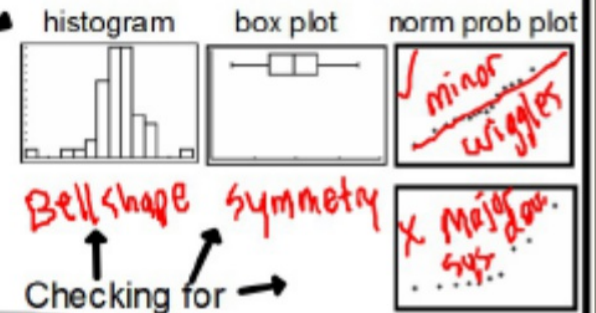
Conditions

Random? \rightarrow yes, stated \checkmark



if conditions are not met... Then

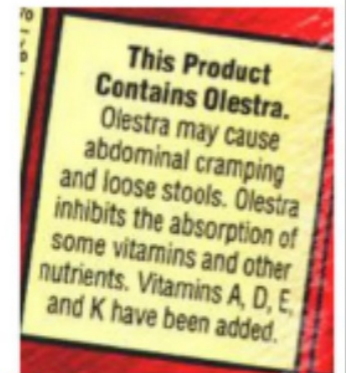
"Proceed w/ caution"



if the P-value is low, the null must go

Interpret

b/c the p-value is low (.037 compared to $\alpha = .05$), we reject the null ($\mu = 328$) in favor of the alternative... the mean olestra is likely > 328 mg. per serving.



NiHiCCI

1 Sample T Test for Means

σ unknown

104 deg	0.5 lb	Simulations - What's the Probability?
if heavily skewed		Least Squares Regression Line... LSRL
nonresponse - bias		Comparing Data Sets (SOCS)
		Surveys - Designing Samples

Learning Card for 2 Sample T-Test

Name

Card #

My girlfriend from Lambert wanted us to attend her Prom instead of North's Prom. I said that I couldn't compete with the Lambert group because they spend much more on average than the North students. To impress her, I pull out my AP Stat skills and come up with the following data: A sample of 18 random Lambert students spent an average of \$345 with a sample standard deviation of 28.5, while a sample of 15 North students revealed an average of \$319 with a sample standard deviation of 41.2. Is there really a difference or is this just due to random chance of different samples?

Name It: *2 Sample t-test for means*

Hypothesize It:

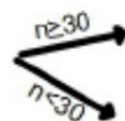
$$H_0: \mu_L = \mu_N \quad H_a: \mu_L > \mu_N$$

or

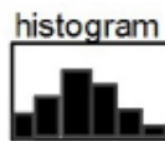
$$\mu_L - \mu_N = 0 \quad \mu_L - \mu_N > 0$$

Conditions: Random? *yes, stated*

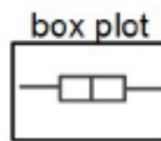
Normal Parent Population?



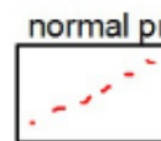
Central Limit Theorem



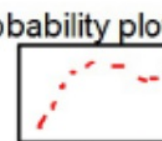
bell shaped unimodal



symmetrical no outliers



minor wiggles ok!



systematic deviations not ok!

Independent? *Are there 2 separate populations?*

Calculations

Test Statistic = $\frac{\text{est diff} - \text{hyp diff}}{SD_{\text{diff}}}$

$$t = \frac{(\bar{X}_L - \bar{X}_N) - (\mu_L - \mu_N)}{\sqrt{\frac{S_L^2}{n} + \frac{S_N^2}{n}}} = \frac{(345 - 319) - 0}{\sqrt{\frac{28.5^2}{18} + \frac{41.2^2}{15}}} = 2.07$$



Interpretation

*P ↓ (.025) vs. α = .05
reject null (no diff).
there is evidence that Lambert spends more!*

P(t > 2.07) = .025

Significance Tests - 2 Sample T-Test (Means)

Least Squares Regression Line... LSRL
Comparing Data Sets (SOCS) of the overall population.
Surveys - Designing Samples

Learning Card for χ^2 (Chi Squared) Test for Homogeneity of Populations

Name

Card #

Is there a difference in the distribution of this categorical data across these various populations or is there homogeneity?

Obs.

	N	S	
Y	50	30	80
N	30	10	40
D	10	20	30
M	40	20	60
	130	40	170

$$E = \frac{r_{total} \times c_{total}}{total}$$

$$E = \frac{8 \times 13}{21}$$

$$E = 4.95$$

2nd Matrix, Edit [A] + Enter observed values E.V.'s calculated [B]

Name it:

Hypothesize It:

H_0 : The dist of the categories is the same for all pop's
 H_A : " " " is Not " " "

Conditions...

All E.V.'s > 1
 $\frac{1}{5} < 5$... no more than $\frac{1}{5}$ of the E.V. can be < 5
 - must have independent SRS's from each pop.

Calculate...

Build your table

observed

expected

$$\frac{(10 - 18.6)^2}{18.6} = 4$$

	N	S
Y	49.5	30.4
N	24.8	15.2
D	18.6	11.4
M	37.7	22.9

Calculate $\chi^2 =$

$$\sum \frac{(O - E)^2}{E} = \frac{(50 - 49.5)^2}{49.5} + \dots = 13.9$$

$$P(\chi^2 > 13.9) = .003$$

Interpret...

Use table to get p-value

df	.25	.20	.15	.10	.05
1	1.32	1.64	2.07	2.71	3.84
2	2.77	3.22	3.79	4.61	5.99
3	4.11	4.64	5.32	6.25	7.81
4	5.39	5.99	6.74	7.78	9.49
5	6.63	7.29	8.12	9.24	11.07

$P \downarrow (.003)$ vs. $\alpha (.05)$
 reject null of no diff...
 there is evidence of a diff. between the populations on this categorical data.

χ^2 (Chi Squared) Test for Homogeneity of Populations

$y = ax + b$, $y = b_0 + b_1x$ Least Squares Regression Line... LSRL

nonresponse - bias by comparing Data Sets (SOCS) of the overall population.

Surveys - Designing Samples

Learning Card for Inference for Linear Regression... Conf Intervals

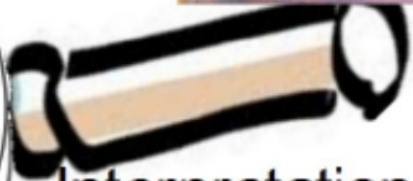
Name

Card #

Stat

Tests

LinRegTInt



Interpretation

We are 95% confident that the interval of (.5, 2.5) contains the true parameter ($\beta \rightarrow$ slope). Stating that for every 1 increase in crycounts we predict IQ increases between .5 + 2.5.

Calculations

Estimate \pm Critical Value \times Std. Dev.
 $b \pm t^* SE_b$ ← always given
 Binomial Setting
 $1.49 \pm 2.042(.487) \rightarrow (.5, 2.5)$
 use t-dist chart w/ df = n - 2

plus

Coincides with the interpretation from the Linear Regression T-Test

take note, zero is not in the interval... there is evidence of a correlation

CICP+

Inference for Linear Regression... Confidence Intervals

0 in the interval?

Least Squares Regression Line... LSRL
 Comparing Data Sets (SOCS) / accurate estimates of the overall population.
 Surveys - Designing Samples

Thank you and go...
fill - in - the - _____!

Blank

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