



Chapter 4 "FRAPPY" {Free Response AP Problem...Yay!}

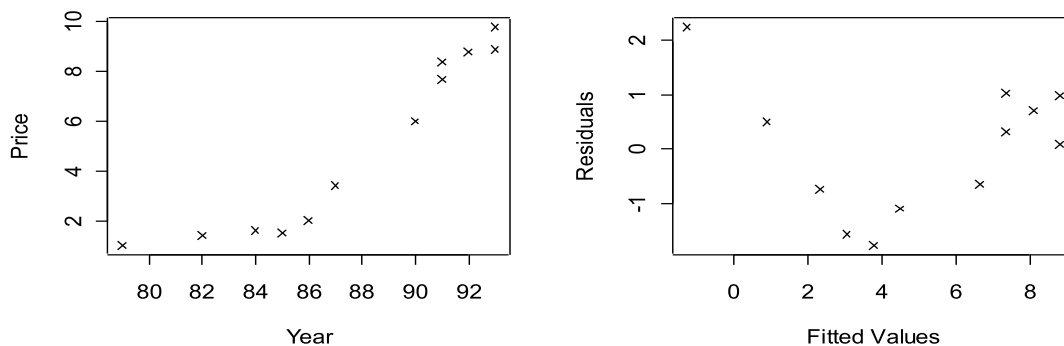
The following problem is taken from an actual Advanced Placement Statistics Examination. Your task is to generate a complete, concise statistical response in 30 minutes - You should expect to spend 30-35 minutes on the "Investigative Task". You will be graded based on the AP rubric and will earn a score of 0-4. After grading, keep this problem in your binder for your AP Exam preparation.

You are planning to sell a used 1988 automobile and want to establish an asking price that is competitive with that of other cars of the same make and model that are on the market. A review of newspaper advertisements for used cars yields the following data for 12 different cars of this make and model. You want to fit a least squares regression model to these data for use as a model in establishing an asking price for your car.

| | | | | | | | | | | | | |
|-------------------------------------|------|------|------|------|------|------|------|------|------|------|------|------|
| Production Year | 1990 | 1991 | 1992 | 1987 | 1993 | 1991 | 1993 | 1985 | 1984 | 1982 | 1986 | 1979 |
| Asking Price (thousands of dollars) | 6.0 | 7.7 | 8.8 | 3.4 | 9.8 | 8.4 | 8.9 | 1.5 | 1.6 | 1.4 | 2.0 | 1.0 |

The computer printouts for three different linear regression models are shown below. Model 1 fits the asking prices as a function of the production year; Model 2 fits the natural logarithm of the asking price as a function of the production year, and Model 3 fits the square root of the asking price as a function of the production year. Each printout also includes a plot of the residuals from the linear model versus the fitted values, as well as additional descriptive data produced from the least squares procedure.

Model 1



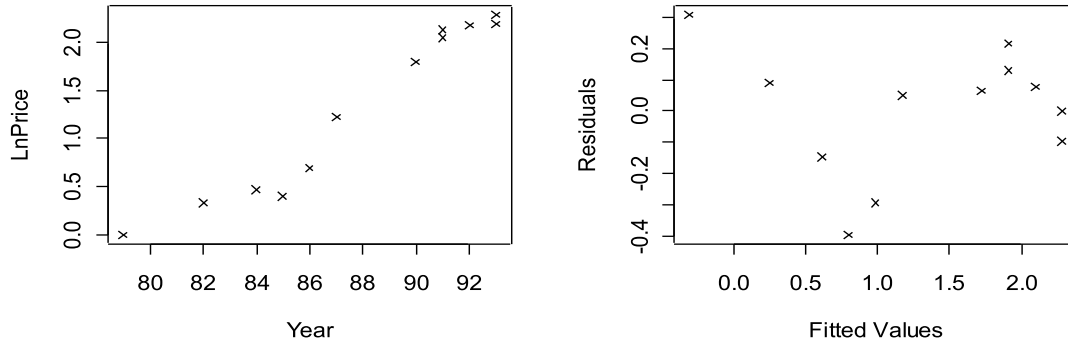
The regression equation is $\text{Price} = -58.1 + 0.719 \text{ Year}$.

$s = 1.255$ $R\text{-sq} = 88.5\%$

| Variable | Coefficient | Stdev | t-ratio | prob |
|----------|-------------|-------|---------|-------|
| Constant | -58.0503 | 7.205 | -8.06 | 0.000 |
| Year | 0.718997 | 0.082 | 8.77 | 0.000 |

| Source | Sum of Squares | df | Mean Square | F-ratio |
|------------|----------------|----|-------------|---------|
| Regression | 121.097 | 1 | 121.097 | 76.9 |
| Residual | 15.7521 | 10 | 1.57521 | |

Model 2



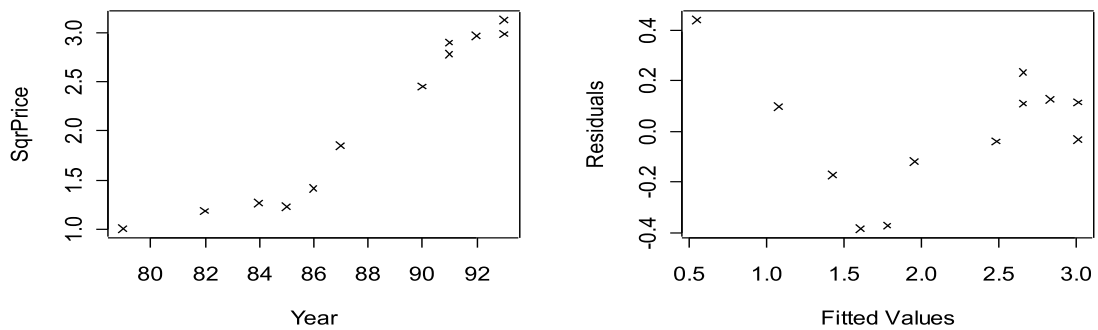
The regression equation is $\text{LnPrice} = -14.9 + 0.185 \text{ Year}$.

$s = 0.213$ $R\text{-sq} = 94.6\%$

| Source | Sum of Squares | df | Mean Square | F-ratio |
|------------|----------------|----|-------------|---------|
| Regression | 8.01898 | 1 | 8.01898 | 177 |
| Residual | 0.453645 | 10 | 0.0453645 | |

| Variable | Coefficient | Stdev | t-ratio | prob |
|----------|-------------|---------|---------|-------|
| Constant | -14.9244 | 1.223 | -12.2 | 0.000 |
| Year | 0.185021 | 0.01392 | 13.3 | 0.000 |

Model 3



The regression equation is $\text{SqrPrice} = -13.3 + 0.176 \text{ Year}$.

$s = 0.252$ $R\text{-sq} = 91.9\%$

| Source | Sum of Squares | df | Mean Square | F-ratio |
|------------|----------------|----|-------------|---------|
| Regression | 7.22212 | 1 | 7.22212 | 114 |
| Residual | 0.635106 | 10 | 0.0635106 | |

| Variable | Coefficient | Stdev | t-ratio | prob |
|----------|-------------|---------|---------|-------|
| Constant | -13.3133 | 1.447 | -9.2 | 0.000 |
| Year | 0.175587 | 0.01647 | 10.7 | 0.000 |

E P I (a) Use Model 1 to establish an asking price for your 1988 automobile.

E P I (b) Use Model 2 to establish an asking price for your 1988 automobile.

E P I (c) Use Model 3 to establish an asking price for your 1988 automobile.

E P I (d) Describe any shortcomings you see in these three models.

E P I (e) Use some or all of the given data to find a better method for establishing an asking price for your 1988 automobile. Explain why your method is better.

Total: __/4